

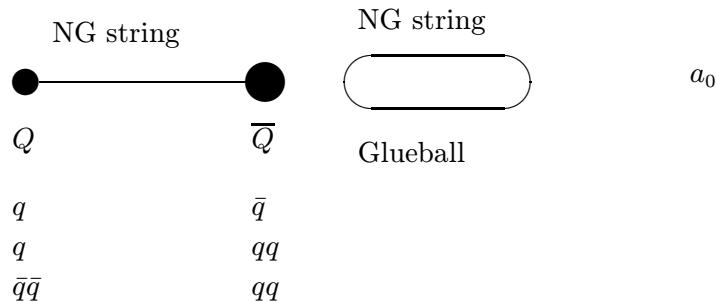
STRING MECHANISM OF CONFINEMENT AND HADRON STRUCTURE

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1. The model of hadrons.
2. $q\bar{q}$ -mesons.
3. Glueballs and the Pomeron trajectory.

The Model



- Relativistic quantum model of hadrons with universal string-tension parameter and current quark masses.
- String contributes to mass and spin of hadrons (current quarks).
- Hadrons lie on Regge trajectories, which depend on universal string tension and current quark (diquark) masses. For light quarks (diquarks) the slope of trajectories is universal.
- Light quarks are relativistic: average quark spins (in polarized hadrons) are twice as small as for nonrelativistic quarks.

$$\begin{aligned} \mathcal{L} = & -a \int_0^{\pi(2\pi)} \sqrt{(\dot{x}\dot{x}')^2 - \dot{x}^2 x'^2} d\sigma + \\ & + \sum_{i=1}^2 \mathcal{L}_i(\dot{x}_i, \xi_i, \lambda_i, m_i) + \mathcal{L}_{ss}; \end{aligned}$$

$$\begin{aligned} x(\sigma, \tau) = & r(\tau) + q(\tau)\cos\sigma; \\ (x(\sigma, \tau) = & r(\tau) + q_1(\tau)\cos\sigma + q_2(\tau)\sin\sigma). \end{aligned}$$

Constraints

Independent variables ζ_i

$$\mathcal{L} = \frac{1}{2} f_{ij} \zeta_i \dot{\zeta}_j - \sum c_k \varphi_k(\zeta),$$

$\varphi_k(\zeta)$ are considered

$$\begin{aligned}\{\zeta_i, \zeta_j\} &= f_{ij}^{-1}, \\ \varphi_k(\zeta) &= 0.\end{aligned}$$

Stability

Quantization $\zeta \rightarrow \hat{\zeta}$ $\{ , \} \rightarrow -i[,]_{\mp}$

$$\begin{aligned}\varphi_k(\hat{\zeta})\Psi &= 0, \\ \varphi_1 &= \sqrt{\vec{J}^2} - K(m^2, m_i^2, a) \rightarrow \\ &\rightarrow \varphi_1 - a_{0n}(m_i, \vec{J}^2, P, C)P_n.\end{aligned}$$

$q\bar{q}$ -mesons

$$\begin{aligned}(\sqrt{\vec{J}^2} - K - \sum_{n=1}^4 a_{0n} P_n)\Psi &= 0, \\ (p_{1\mu} \gamma^\mu - m_1)\Psi &= 0, \\ \Psi(p_{2\mu} \gamma^\mu + m_2) &= 0;\end{aligned}$$

$$\Psi \equiv \Psi_n = (\Psi_{jMLS}(\vec{n}))_{\alpha\beta},$$

$$\sqrt{j(j+1)} = K + a_{0n},$$

$$a = 0.176 \pm 0.002 \text{ GeV}^2,$$

$$m_s = 224 \pm 7 \text{ MeV}, \quad m_c = 1440 \pm 10 \text{ MeV},$$

$$m_b = 4715 \pm 20 \text{ MeV},$$

$$m_u/m_d = 0.55, \quad m_s/m_d = 20.1,$$

$$m_u = 6.2 \pm 0.2 \text{ MeV}, \quad m_d = 11.1 \pm 0.4 \text{ MeV},$$

$$a_{0n}.$$

Glueballs and the Pomeron trajectory

$$\vec{J} = \vec{L}_1 + \vec{L}_2,$$

$$(\sqrt{\vec{L}_1^2} + \sqrt{\vec{L}_2^2} - \frac{1}{4\pi a}m^2 - a_0)\Psi = 0,$$

$$(\sqrt{\vec{L}_1^2} - \sqrt{\vec{L}_2^2})\Psi = 0.$$

$$\begin{aligned}\Psi_{jMl}(\vec{n}_1, \vec{n}_2) &= \sum C(jM, lm_1, lm_2) Y_{lm_1}(\vec{n}_1) Y_{lm_2}(\vec{n}_2), \\ l &= 1, 2, 3, \dots, \\ j &= 0, \dots, 2l, \\ I^G j^{PC} &= 0^+ j^{++}.\end{aligned}$$

$$\begin{aligned}f_0(1500), \quad 0^+0^{++}, \quad m &= 1500 \pm 10 \text{ MeV}, \\ f_1(1510), \quad 0^+1^{++}, \quad m &= 1518 \pm 5 \text{ MeV}, \\ f_2(1565), \quad 0^+2^{++}, \quad m &= 1542 \pm 22 \text{ MeV}.\end{aligned}$$

$$\begin{aligned}m_1 &= 1500 \pm 20 \text{ MeV}, \\ a_0 &= 1.81 \pm 0.04,\end{aligned}$$

$$\begin{aligned}0^{++}, 1^{++}, 2^{++}, 3^{++}, 4^{++}; \quad m_2 &= 2610 \pm 20 \text{ MeV}. \\ 0^{++}, 1^{++}, \dots, 5^{++}, 6^{++}; \quad m_3 &= 3360 \pm 25 \text{ MeV}.\end{aligned}$$

$$\begin{aligned}j &= 2l - k, \\ \sqrt{(j+k)(j+k+2)} &= \frac{1}{4\pi a}m^2 + a_0.\end{aligned}$$

The Pomeron trajectory $k = 0$

$$j(m^2) = \sqrt{\left(a_0 + \frac{1}{4\pi a}m^2\right)^2 + 1} - 1,$$

$$j(0) = 1.07 \pm 0.03.$$

$\Psi_k(\xi)$ are considered

$$\begin{aligned}\xi_i, \xi_j &= f_{ij}^{-1}, \\ \varphi_k(\xi) &= 0,\end{aligned}$$

$$\begin{array}{l} \text{Quantization } \xi \rightarrow \hat{\xi} \\ \{ \} \rightarrow -i[]_{\mp} \end{array}$$

$$\begin{gathered}\Phi_k(\hat{\xi})\Psi=0,\\\varphi_1=\sqrt{\vec{J}^2}-K(m^2,m_i^2,a)\rightarrow\varphi_1-a-0(m_i,\vec{J}^2,P,C)P_n).\end{gathered}$$

$$q\bar q\text{-mesons}$$

$$(\sqrt{\vec{J}^2}-K-\sum_{n=1}^4a_{0n}P_n)\Psi=0,$$

$$(p_{1\mu}-\gamma^\mu-m_1)\Psi=0,$$

$$\Psi(p_{2\mu}+m_2)=0,$$

$$\Psi\equiv\Psi_n=(\Psi_{jMls}(\vec{n}))_{\alpha\beta},$$

$$\sqrt{j(j+1)}=K+a_{0n},$$

$$a=0.176\pm 0.002~(GeV^2),$$

$$m_s = 224 \pm 7~MeV,~ m_c = 1440 \pm 10~MeV,$$

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